

tation. This, however, is merely answerable to the complexity of the physical problem, and no simpler general solution can possibly exist.

The foregoing method when applied to the differential equations of the transmission line, leads to the following differential equations

$$\begin{aligned}(Lp + R)J &= -\frac{\partial}{\partial x}\Phi + LI^0, \\ (Cp + G)\Phi &= -\frac{\partial}{\partial x}J + CV^0.\end{aligned}\tag{11}$$

Here J and Φ are Laplace transforms of the current I and voltage V and I^0 , V^0 are the initial values of I and V at reference time $t = 0$. J , Φ , I^0 , V^0 are functions of x but of course independent of t .

The formal solution of equations (11) is as follows: write

$$\begin{aligned}Lp + R &= Z(p) = Z, \\ Cp + G &= Y(p) = Y, \\ \sqrt{ZY} &= \gamma, \quad \sqrt{Z/Y} = K.\end{aligned}\tag{12}$$

Also

$$LI^0 - \frac{C}{Y} \frac{\partial}{\partial x} V^0 = F(x) = F.$$

Then

$$\begin{aligned}J &= e^{-\gamma x} \left\{ A + \frac{1}{2K} \int^x dy F(y) e^{\gamma y} \right\} \\ &- e^{\gamma x} \left\{ B + \frac{1}{2K} \int^x dy F(y) e^{-\gamma y} \right\},\end{aligned}\tag{13}$$

$$\Phi = -\frac{K}{\gamma} \frac{\partial}{\partial x} J + \frac{C}{Y} V^0.\tag{14}$$

A and B are constants of integration determined by the relations between J and Φ at the physical terminals of the line.